
Piezooptical constants of Rochelle salt crystals

V.Yo. Stadnyk, M.O. Romanyuk, V.Yu. Kurlyak, V.F. Vachulovych

Ivan Franko L'viv National University, 8 Kyryl and Mefodiy Str., L'viv, 79005, Ukraine

Received 26.08.1999

Abstract

The influence of uniaxial mechanical pressure applied along the principal axes and the corresponding bisectors on the birefringent properties of Rochelle salt (RS) crystals are studied. The temperature (77-300 K) and spectral (300-700 nm) dependencies of the effective π_{im}^0 and absolute π_{im} piezooptical constants of the RS crystals are calculated. The intercept of dispersion curves of π_{im} is revealed in the region of the birefringence sign inversion. This testifies that the anisotropy of the piezooptical constant tensor decreases there. The temperature dependencies of absolute piezooptical constants do not manifest notable anomalies in the region of phase transitions of the Rochelle salt

Key words: uniaxial mechanical pressure, birefringence, combined and absolute piezooptical constants

PACS: 78.20.Fm, 78.20.H, 61.50.Ks

Elastooptical properties of the Rochelle salt (RS) crystals have been investigated by different authors. Those properties have been measured for the first time by Pockels [1] who determined only the order of magnitude for three of 12 piezooptical constants, namely the constants π_{44} , π_{55} and π_{66} . Using the technique of localized interference bands, Narasimhamurthy have determined the whole matrix of the absolute piezooptical constants at $T = 27^\circ\text{C}$ (orthorhombic symmetry) for the yellow sodium spectral line [2]. Temperature variations of the effective piezooptical constants in the RS crystals measured with the half-wave voltage technique have been completely studied in the [3, 4].

The aim of this investigations is to determine the temperature (77-300K) and

spectral (300-700 nm) dependencies of the absolute piezooptical constants of the RS crystals.

The influence of the uniaxial pressure on the temperature and spectral variations of the birefringence was studied with registering the changes in the interference pattern obtained with the spectrograph DFS-8. The instrument provides spatial resolution of extrema of different orders.

It was determined that uniaxial pressure σ_m ($m = X, Y, Z$) leads to different character and values of the Δn_i changes. For example, the Δn_z birefringence increases by 4.1×10^{-5} at the pressure $\sigma_x = 150$ bar but decreases by 3.9×10^{-5} in the case of the pressure $\sigma_x = 150$ bar. It is revealed that the pressure sensitivity of Δn_i increases with decreasing wavelength.

In the RS crystals, an inversion in the birefringence sign (IBS) exists along the X-axis (the direction of the acute bisector between the optical axes) [5]. The action of the uniaxial pressure σ_x or σ_z leads to similar behaviour of the birefringence Δn_x ($\delta\Delta n_x = 2.2 \times 10^{-5}$ for $\sigma_z = 150$ bar, and -2.9×10^{-5} for $\sigma_x = 150$ bar). At room temperature, the sign of birefringence changes ($\Delta n_x = 0$) in the non-stressed sample at $\lambda = 285$ nm. The pressure σ_z shifts the IBS point towards the long-wavelength region ($\Delta n_x = 0$ at $\lambda = 270$ nm), while in the case of the pressure σ_x the IBS point shifts towards the long-wavelength region ($\Delta n_x = 0$ at $\lambda = 308$ nm). A significant increase in the pressure sensitivity of Δn_x is observed in the spectral region of the IBS ($\delta\Delta n_x = 6.9 \times 10^{-5}$ at $\sigma_z = 150$ bar, and -6.5×10^{-5} at

$\sigma_x = 150$ bar for $T = 294$ K and $\lambda = 300$ nm). The phenomenon will be discussed below.

The effective difference of piezooptical constants was calculated using the formula

$$\pi_{im}^0 = \frac{2\delta\Delta n_i}{\sigma_m} - 2\Delta n_i s_{im} \quad (1)$$

where $\delta\Delta n_i$ is the induced birefringence for the light propagation direction parallel to the i axis, σ_m the mechanical pressure along the m axis, i and m the principal axes of the optical indicatrix, and s_{im} the elastic coefficients. The second term in formula (1) describes the contribution caused by the pressure-imposed changes in the sample dimensions along the light propagation direction. The s_{im} data for the calculations are given in the papers [6, 7].

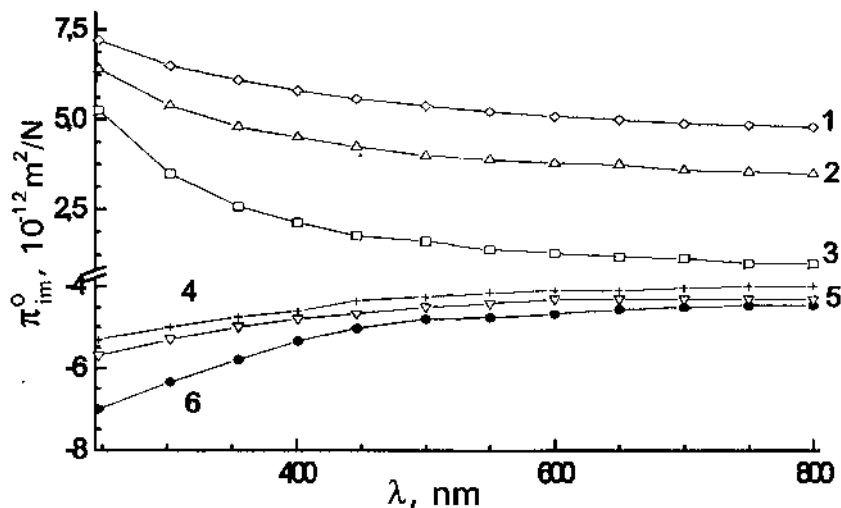


Fig.1. Dispersion of the combined piezooptical constants of Rochelle salt crystal at $T = 298$ K: 1 - π_{32}^0 ; 2 - π_{23}^0 ; 3 - π_{13}^0 ; 4 - π_{21}^0 ; 5 - π_{31}^0 ; 6 - π_{12}^0 .

Dispersion dependencies of π_{im}^0 at room temperature are shown in fig. 1. The sign of π_{im}^0 is considered as positive if the birefringence Δn_i increases under the influence of the pressure σ_m . As is seen from the figure, the π_{32}^0 , π_{23}^0 and π_{13}^0 coefficients are positive, while the π_{12}^0 , π_{31}^0 and π_{21}^0 are negative. The absolute values of π_{im}^0 change with decreasing wavelength, i.e.

a pronounced dispersion of piezooptical constants occurs. Probably, the dispersion is caused by the fact that, under the action of the uniaxial pressure, the shift of the fundamental absorption edge (in the RS crystals at the room temperature it is located at $\lambda = 247$ nm) takes place in the vicinity of that edge. This leads to a notable dispersion of π_{im}^0 .

Especially strong dispersion is observed in the case of the π_{13}^0 and π_{12}^0 constants:

$$\begin{aligned} d\pi_{13}^0/d\lambda &= -3.3 \times 10^{-2} \text{ Br/nm} \quad \text{and} \\ d\pi_{12}^0/d\lambda &= 1.5 \times 10^{-2} \text{ Br/nm.} \end{aligned}$$

The piezooptical constants π_{13}^0 and π_{12}^0 correspond to the changes in the birefringence Δn_x under the influence of the uniaxial pressures σ_x and σ_z . Since an IBS exists in x - direction in the RS, notable increase of π_{12}^0 and π_{13}^0 within the

spectral range of the IBS may testify about a significant increase in the sensitivity of IBS with respect to the uniaxial pressures.

Temperature dependencies of the π_{im}^0 coefficients for the RS crystals are shown in fig. 2. All the measured constants exhibit insignificant anomalies in the course of the PT, specifically a slight change in the curve slopes is observed.

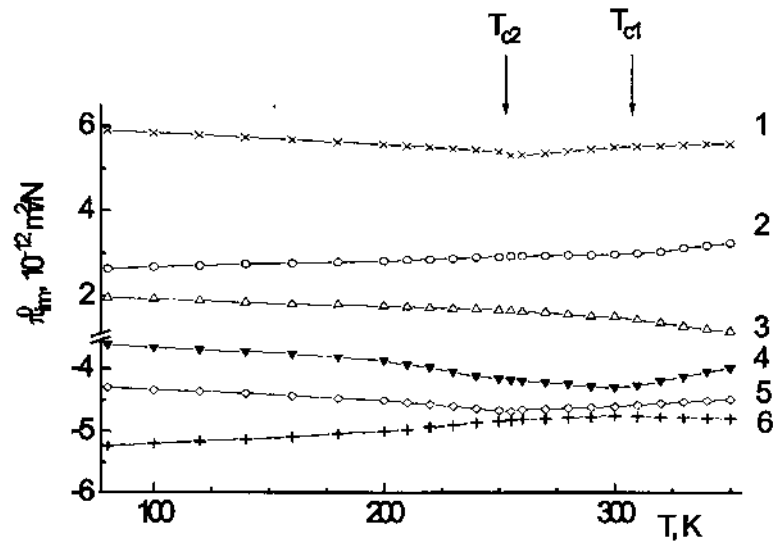


Fig. 2. Temperature dependencies of combined piezooptical constants of Rochelle salt crystal for $\lambda=500$ nm: 1 - π_{32}^0 ; 2 - π_{23}^0 ; 3 - π_{13}^0 ; 4 - π_{21}^0 ; 5 - π_{31}^0 ; 6 - π_{12}^0 .

In the paraelectric phase ($T < 255$ K and $T > 297.5$ K) the crystal structure is described by the point symmetry group 222, so that we have used the reported temperature and spectral dependencies of the effective piezooptical constants for the RS crystals, as well as the known relations for the piezooptically induced birefringence in the orthorhombic crystals (the ordinary Pockels' method [1]) in order to calculate the spectral and temperature dependencies of the absolute piezooptical constants of the RS crystals.

For this aim we have solved the system of nine equations of the following type:

$$\pi_{im}^0 = \frac{n_m^3 \pi_{mm} - n_j^3 \pi_{jm}}{2} \quad (2)$$

where the π_{im} are the unknown quantities, n_i , n_j and n_m the absolute refractive indices for the

given light wavelength and temperature are used from the reference [8].

The dispersion dependencies of the absolute piezooptical constants π_{im} in the RS crystals are shown in fig.3. As it is seen from the figure, the dispersion of the piezo-constants is normal, and is equal to $d\pi_{im}/d\lambda = 3.3$, 7.5 and 6.0 for $im = 11, 21, 31$ (that being corresponding to the pressure σ_x), 4.0, 2.8 and 3.2 for $im = 12, 22, 32$ (the pressure σ_y) and 3.7, 0.9 and 1.5 for $im = 13, 23, 33$ (the pressure σ_z), respectively. It is worthwhile to point out a following interesting detail. The extrapolation of the curves π_{23} and π_{33} (the same about π_{32} and π_{22}) into the short-wavelength region yields in their intersection, i.e. to their equality in the region 280 nm. This corresponds to the spectral position of the IBS at the room temperature.

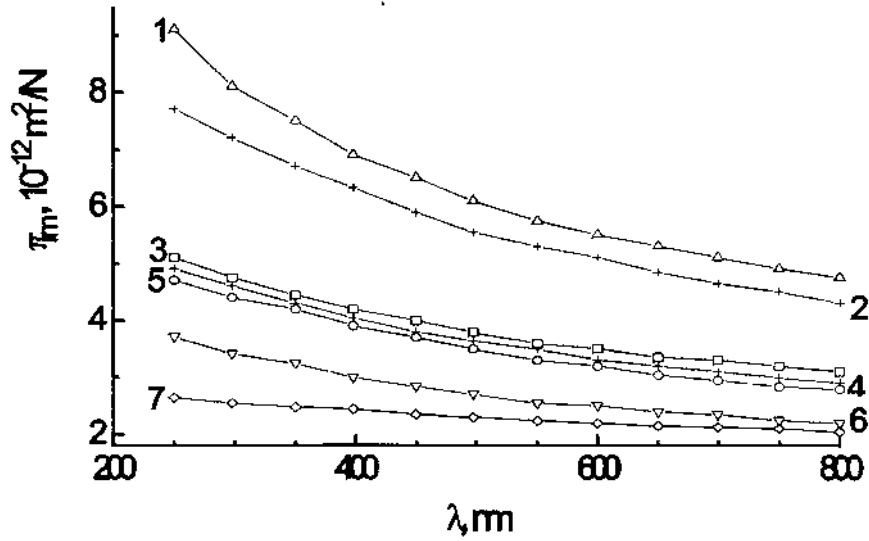


Fig.3. Dispersion of the absolute piezooptic constants of Rochelle salt crystal at T=298K:

1 - π_{21} ; 2 - π_{31} ; 3 - π_{12} ; 4 - π_{11} ; 5 - π_{32} ; 6 - π_{23} ; 7 - π_{33} .

The piezooptic constants π_{23} and π_{33} are responsible for the variation of refractive indices n_y and n_z under the action of the pressure σ_z . Those refractive indices determine the birefringence Δn_x in the direction of the IBS. Quite similarly, the constants π_{23} and π_{32} determine the variation of n_y and n_z when σ_x is acting. Thus, a decreasing of the anisotropy of piezooptic constant tensor occurs in the vicinity of the IBS, the phenomenon which has been earlier detected in the LiKS0_4 crystals [9].

Fig. 4 represents the temperature dependence of the absolute piezooptic constants of the RS crystals for the wavelength $\lambda=500$ nm. It is clearly seen that the anomalies in $\pi_{im}(T)$ are practically not revealed at the upper PT. The anomalies in $\pi_{im}(T)$ in the course of the lower PT are insignificant. In general, the π_{im} are only slightly temperature dependent, except for the π_{21} and π_{31} .

The absence of the pronounced anomalies in $\pi_{im}(T)$ for the RS crystals are easy to explain using the relationships, which describe the anomalies of piezooptic constants:

$$\delta\pi_{im} = -\frac{2}{n_i^3} \frac{\delta n_i^s}{\sigma_m} = -\frac{2}{n_i^3} \frac{dT_c}{d\sigma_m} \frac{dn_i^s}{dT} \quad (3)$$

The coefficients $dT_c/d\sigma_m$, which characterize the shift of the PT point under the pressure, are equal to 0.005 K/bar. The spontaneous polarization and spontaneous electrooptical effect determining the value of dn_i^s/dT at the PT are also insignificant. This is why the value $d\pi_{im}$ turns out to be small and is of the order of magnitude comparable with the experimental accuracy for π_{im} .

Hence the temperature dependencies of the π_{im} coefficients in the RS crystals are mainly caused by the "true" piezooptic contribution and, consequently, do not have any remarkable step-like anomalies.

Thus, we have revealed that the birefringence in the RS crystals is sensitive to the uniaxial pressure along the principal axes of optical indicatrix. Less sensitivity is characteristic with respect to the pressure directed along the directions of the corresponding bisectors. The calculated spectral dependencies of the effective and absolute piezooptic constants of the RS crystals manifest a notable dispersion in the ultraviolet spectral region. This is caused by the influence of uniaxial pressure on the position of the fundamental absorption edge. We have detected

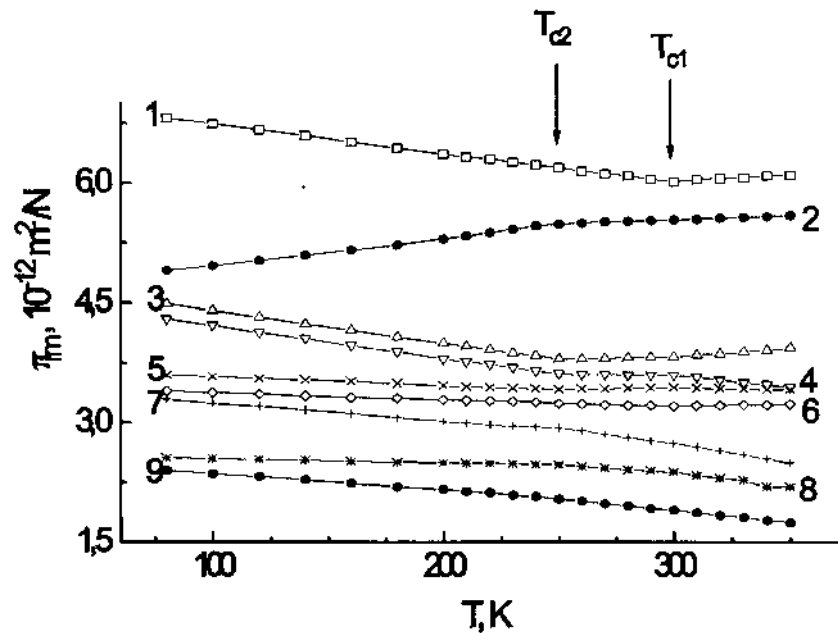


Fig.4. Temperature dependences of absolute piezooptical constants of Rochelle salt crystal for $\lambda=500$ nm: 1 - π_{21} ; 2 - π_{31} ; 3 - π_{12} ; 4 - π_{11} ; 5 - π_{13} ; 6 - π_{32} ; 7 - π_{22} ; 8 - π_{23} ; 9 - π_{33} .

the intersection of the dispersive curves π_{23} and π_{33} , as well as π_{22} and π_{32} , in the region of the birefringence sign inversion, which testifies that the anisotropy of the piezooptical constant tensor of a rank four becomes lower within the region of the isotropic point. The temperature dependencies of the absolute piezooptical constants do not reveal clearly expressed anomalies in the region of the PT in RS, thus testifying the fact that the temperature dependences of the π_{im} coefficients originate mainly from the “true” piezooptical contribution.

References

1. Narasimhamurty T. Photoelastic and electrooptic properties of crystals. M.: Mir, 1984. (in Russian)
2. Narasimhamurty T. // Phys. Rev., 1969, vol. 186. No 3, P. 945.
3. Romanyuk M.O., Mycyk B.G. // Fiz. Electr. L'viv, 1982, vol. 42, P. 66. (in Russian)
4. Mycyk B.G. // Optika Aniz. Sred. M.: Mir, 1988, P. 99. (in Russian)
5. Romanyuk M.O., Gaba V.M., Kostecticky O.M. // Optika i spectr., 1983, vol. 54, No 1, P. 186. (in Russian)
6. Vergnoux A.M., Blanc J., Viere R. // Comptes. Renduc. Acad., 1957, vol. 244, P. 580.
7. Zheludev I.S. Fizika krist. dielectr. M.: Nauka, 1968. (in Russian)
8. Romanyuk M.O., Gaba V.M., Kostecticky O.M. // Kristallografiya, 1980, vol. 25, No 5, P. 1076. (in Russian)
9. Romanyuk M.O., Stadnyk V.Yo. // Ukr. Fiz. Zhur., 1996, vol. 41, No 2, P. 232. (in Russian)